

Code Applications and Data

Lecture 3

2/9/17

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fBmMLE.m: input

- First input is an $N \times 2$ matrix of x and y positions
- Second input is dt (aka the shortest lag time)
- Third input is dt
 - This is an easy way for the code to assume a linear drift

fBmMLE.m: output

- [mle, ci]
- “mle.Sigma” is a 2x2 matrix. To transform to D, do: $(\text{Sigma}(1,1) + \text{Sigma}(2,2))/4$
 - Sigma here is actually sigma squared, where $D = .5 * \text{sigma}^2$
- “mle.Beta” are the drift parameters in each coordinate
- “mle.alpha” is alpha

“other analytics”

- brownianMLE.m – finds MLE of D and drift params, μ , for brownian paths
- path_MSD.m – computes MSD for a single path at optimal lag times
- fBmXY_HD.m – simulates fBm paths (can be used to simulate brownian paths as well)
- ellipse.m – calculates confidence ellipses (for (D, α) distributions) using principal components
- dimless.m – non-dimensionalizes D
- Moduli.m – transforms MSD into the viscous and elastic moduli by the generalized Stokes-Einstein relation (Mason-Weitz 1996)
 - spline_der.m – used for spline interpolation of the MSD in Moduli.m

path_MSD.m

- `[msd, lags] = path_MSD(data, frame_rate)`
- To plot: `plot(lags, msd)`
 - `set(gca, 'xscale', 'log'); set(gca, 'yscale', 'log')`

ellipse.m

- To plot the output: `plot(exp(e(1,:)), e(2,:))`, since the ellipse is fitting data that has a semi-log scaling

dimless.m

- Outputs a non-dimensionalized value for D (no units, like α), and requires as input: α , dimensional D (from mle fit) and bead diameter, which will be 1 for our experiments

Moduli.m: input

- First argument is a $2 \times M$ matrix of MSD (top row) and the corresponding lag times (second row)
- Second argument is the number of points used in the spline interpolation (use 200)

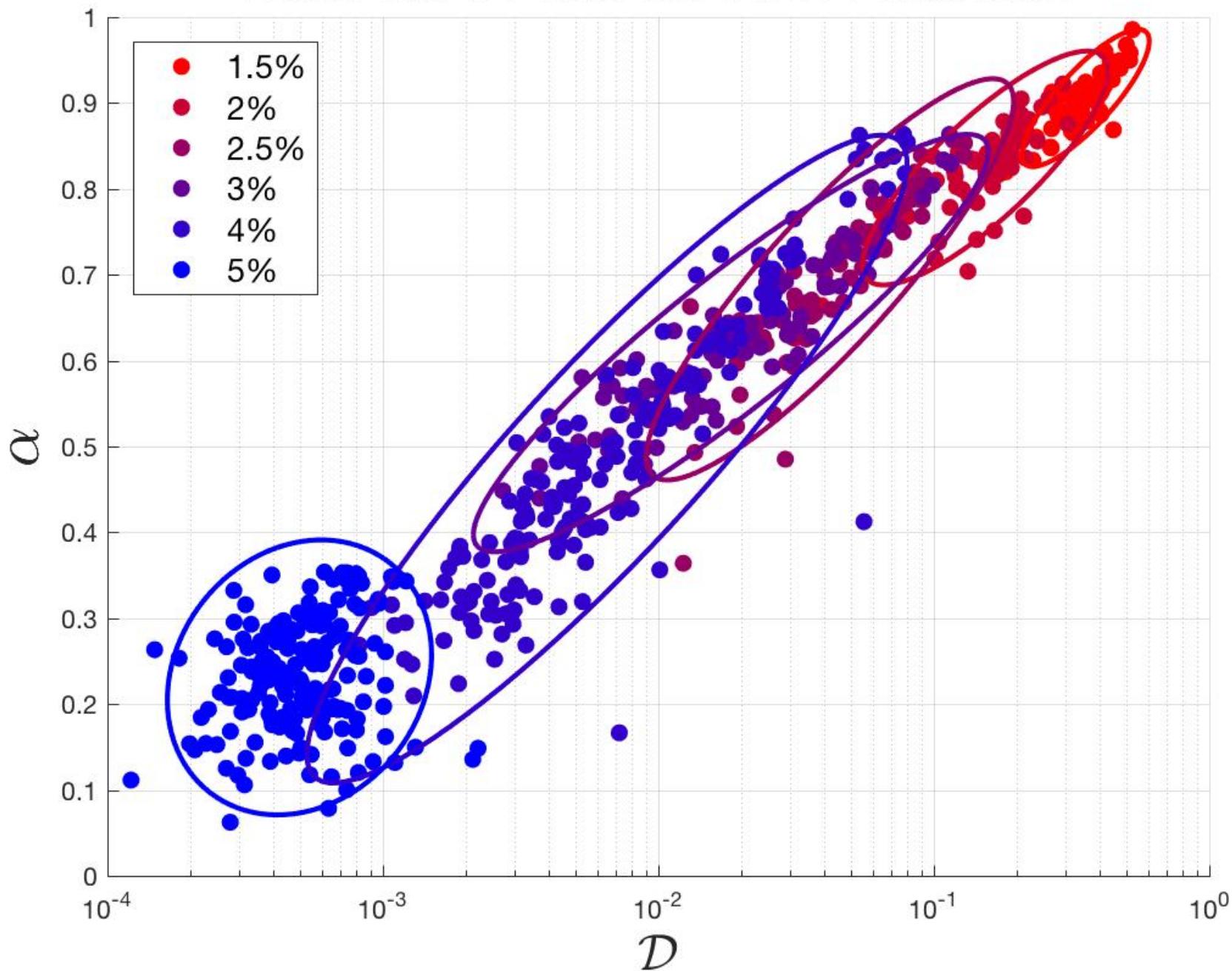
Moduli.m: output

- First is G' (elastic modulus)
- Second is G'' (viscous modulus)
- Third is ω (frequency)
- When plotting, we need to convert ω to radians, so transform the frequency to $\rightarrow 2*\pi*\omega$

The Dataset

- HBE mucus: Several different weight percents of cell culture mucus (the same used in the PLoS ONE paper). Mucus is heterogeneous.
 - Frame rate = 60 fps
 - Bead diameter = 1 micron
 - Try to recreate the following figure:

fBm MLE fits to HBE Mucus



Papers

- How MLE works: JOR Mellnik et al 2016
 - <https://arxiv.org/pdf/1509.03261.pdf>
- PLoS ONE HBE mucus: PLoS ONE Feb 2014 Hill et al
 - <http://journals.plos.org/plosone/article?id=10.1371/journal.pone.0087681>